Preparing for the Final
Dec 13, 4:00-6:00, ICS174

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ICS 271

Fall 2018

Basics

- 2 hours
- closed-book
- 1 (one) sheet of A4 size paper of notes

- To pass MS comprehensive, must get at least B

Material Covered

- Chapters 3-10
  - Search
  - Games
  - Constraint Satisfaction
  - Propositional Logic
  - First Order Logic
  - Classical Planning
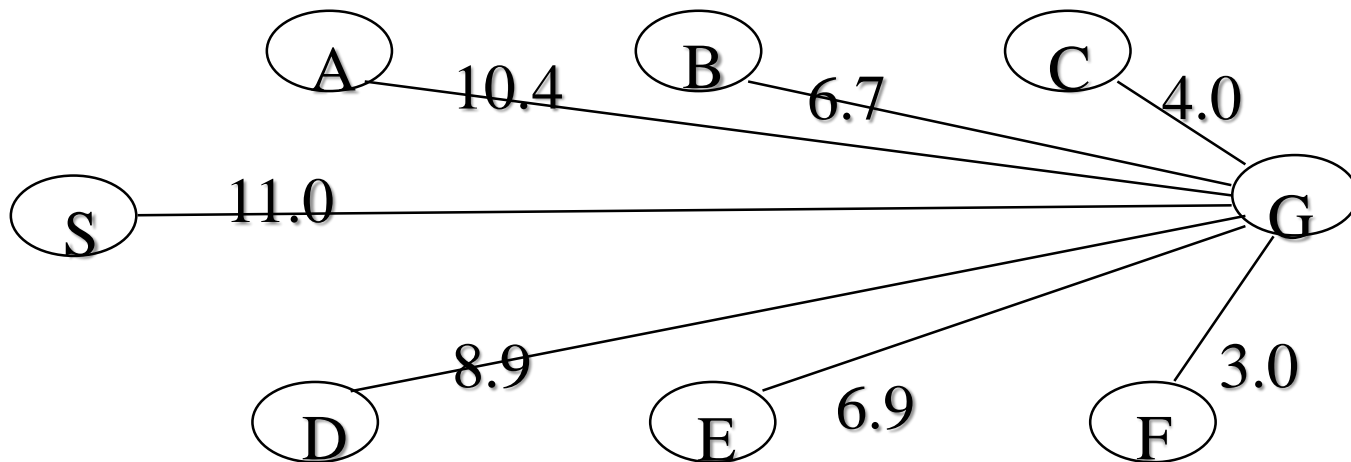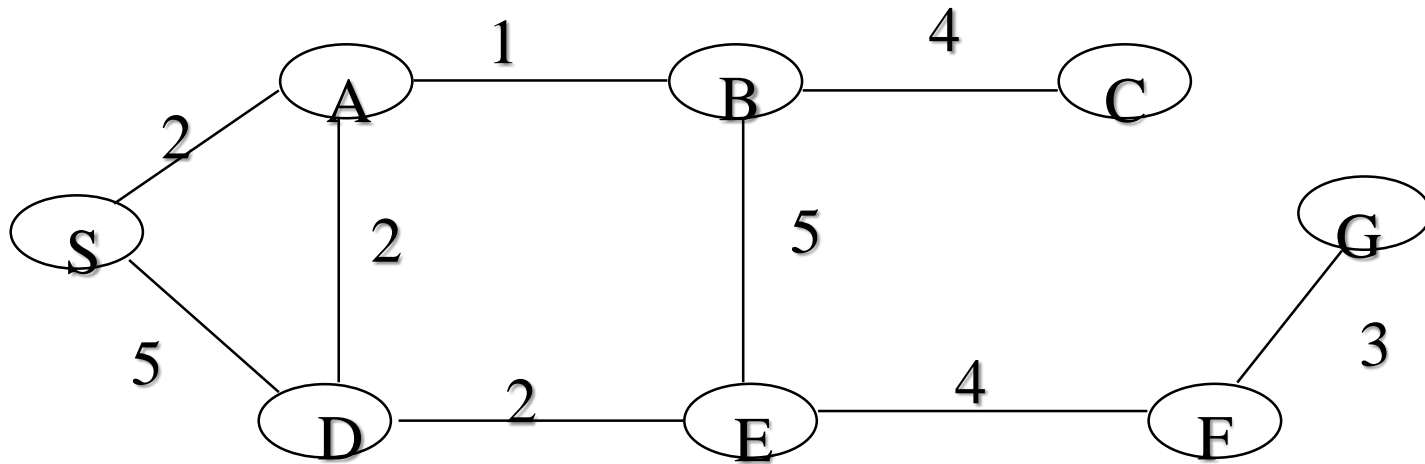- Only material we covered in class (lecture)

Exam

- Section of TRUE/FALSE questions
  - e.g. "Arc consistent problem with non-empty variable domains is guaranteed to have a solution?"
- Sections
  - (Heuristic) Search
  - Games
  - Constraint Satisfaction
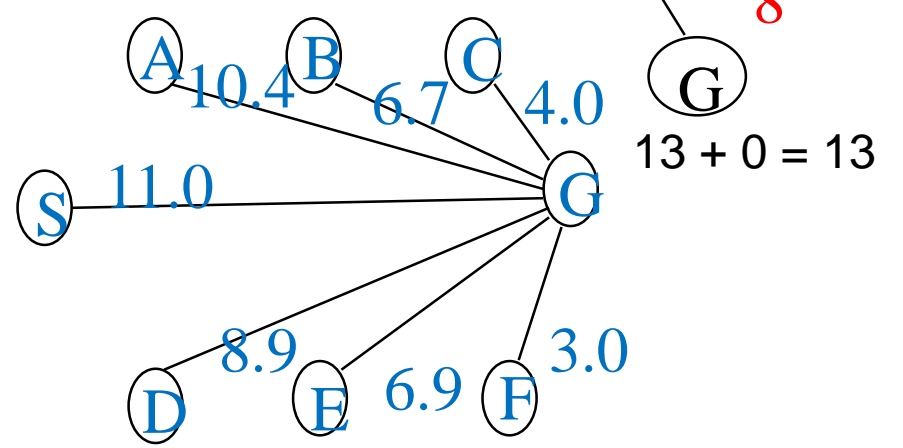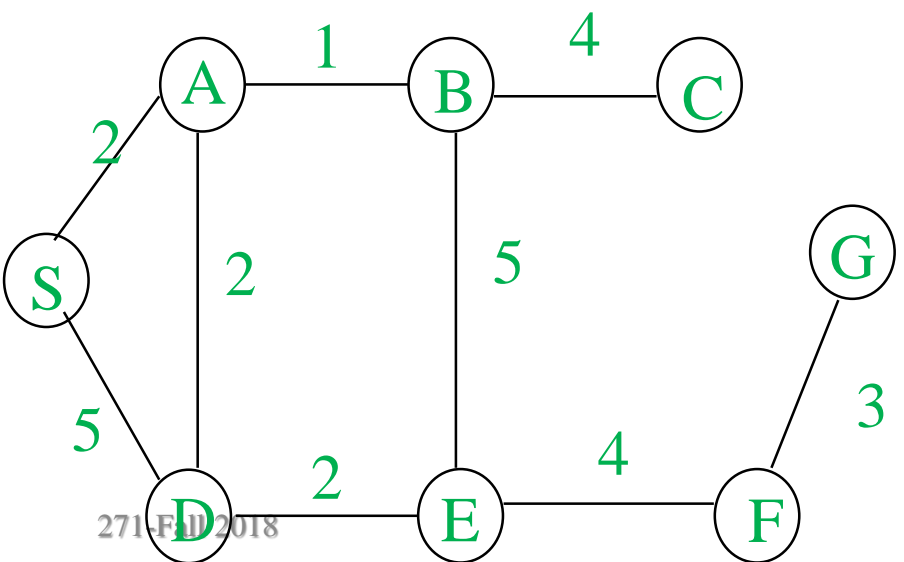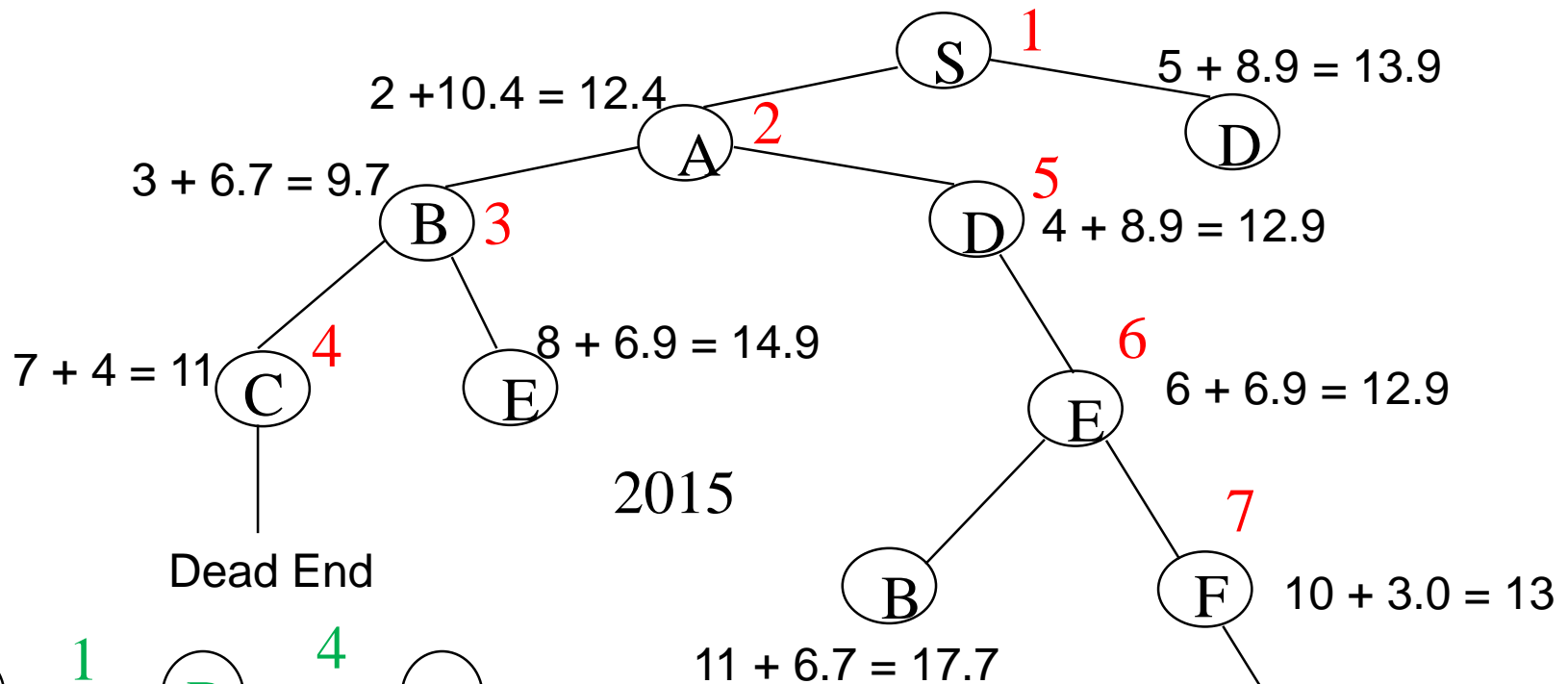 - (First Order) Logic
  - Classical Planning

Chapters 3,4 (Search) Concepts

- Search space : states (initial, goal), actions
- Search tree/graph
- Breadth-first, depth-first, uniform-cost search
  - Expanding a node, open (frontier), closed (explored) lists
  - Optimality, complexity
  - Depth limited search, iterative deepening search
- Heuristic search
  - Heuristic fn, admissibility, consistency
  - f, h, g, h*, g*, C*
  - Heuristic dominance
- Greedy search
- A*, IDA*
- Branch-and-Bound DFS
- Generating heuristics from relaxed problems
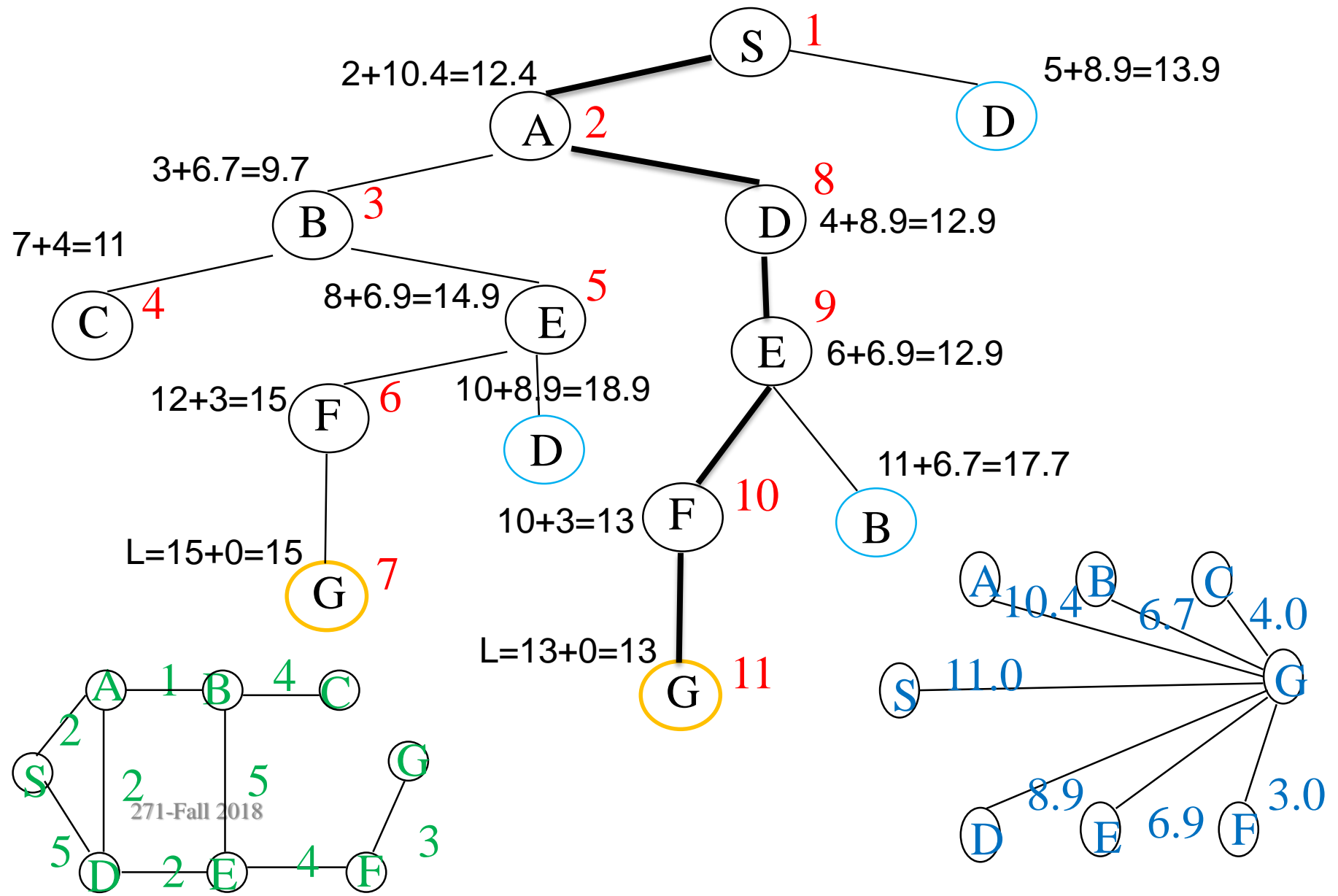- Hill-climbing search, SLS, local vs. global maxima

Search Problem

A —1— B —4— C

2 (S-A)

2 (A-D)

5 (S-D)

5 (B-E)

S

G

3 (G-F)

D —2— E —4— F

A —10.4— G

B —6.7—

C —4.0

S —11.0— G

D —8.9

E —6.9

F —3.0

Example of A* Algorithm in Action

S 1

5 + 8.9 = 13.9

2 +10.4 = 12.4

A 2

D

3 + 6.7 = 9.7

B 3

D 5

4 + 8.9 = 12.9

8 + 6.9 = 14.9

7 + 4 = 11

C 4

E

E 6

6 + 6.9 = 12.9

2015

Dead End

B

F

10 + 3.0 = 13

11 + 6.7 = 17.7

7

8

A   1   B   4   C

G

2

A 10.4   B   C

6.7   4.0

G

2

5

S 11.0   G

13 + 0 = 13

S

5

3

8.9   3.0
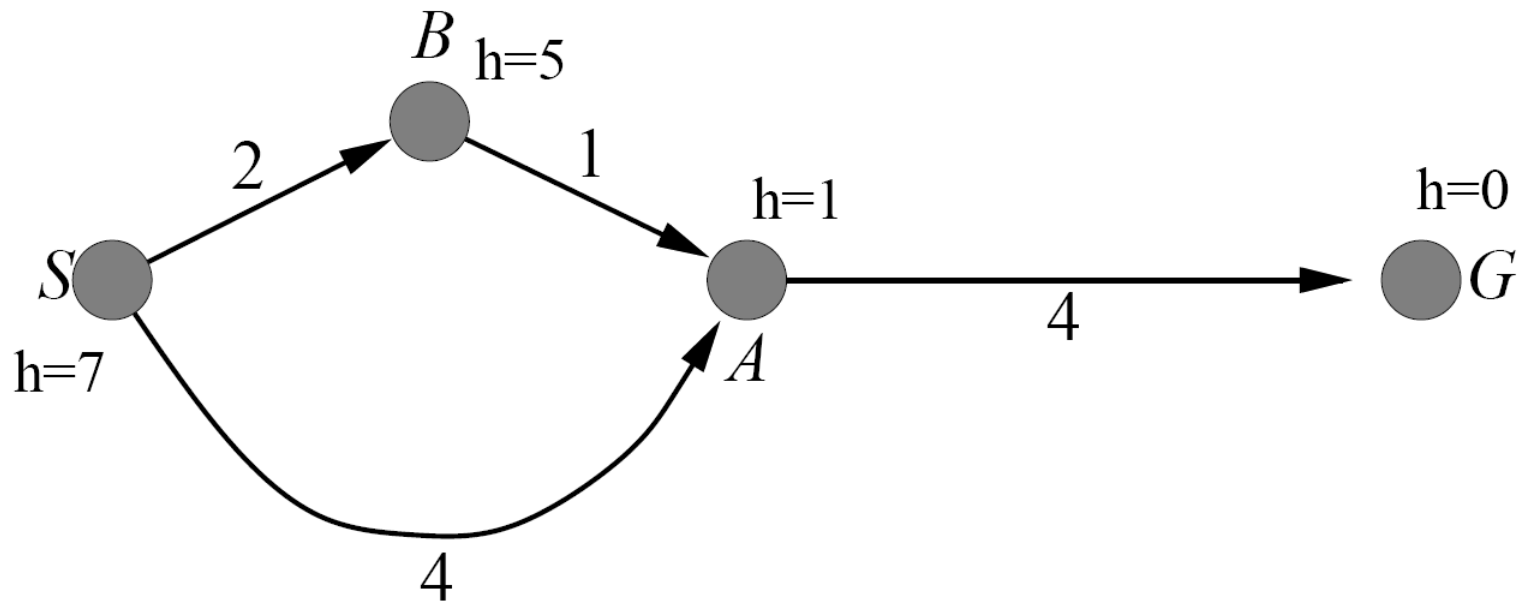
D   2   E   4   F

D   E   6.9   F

Example of Branch and Bound in action
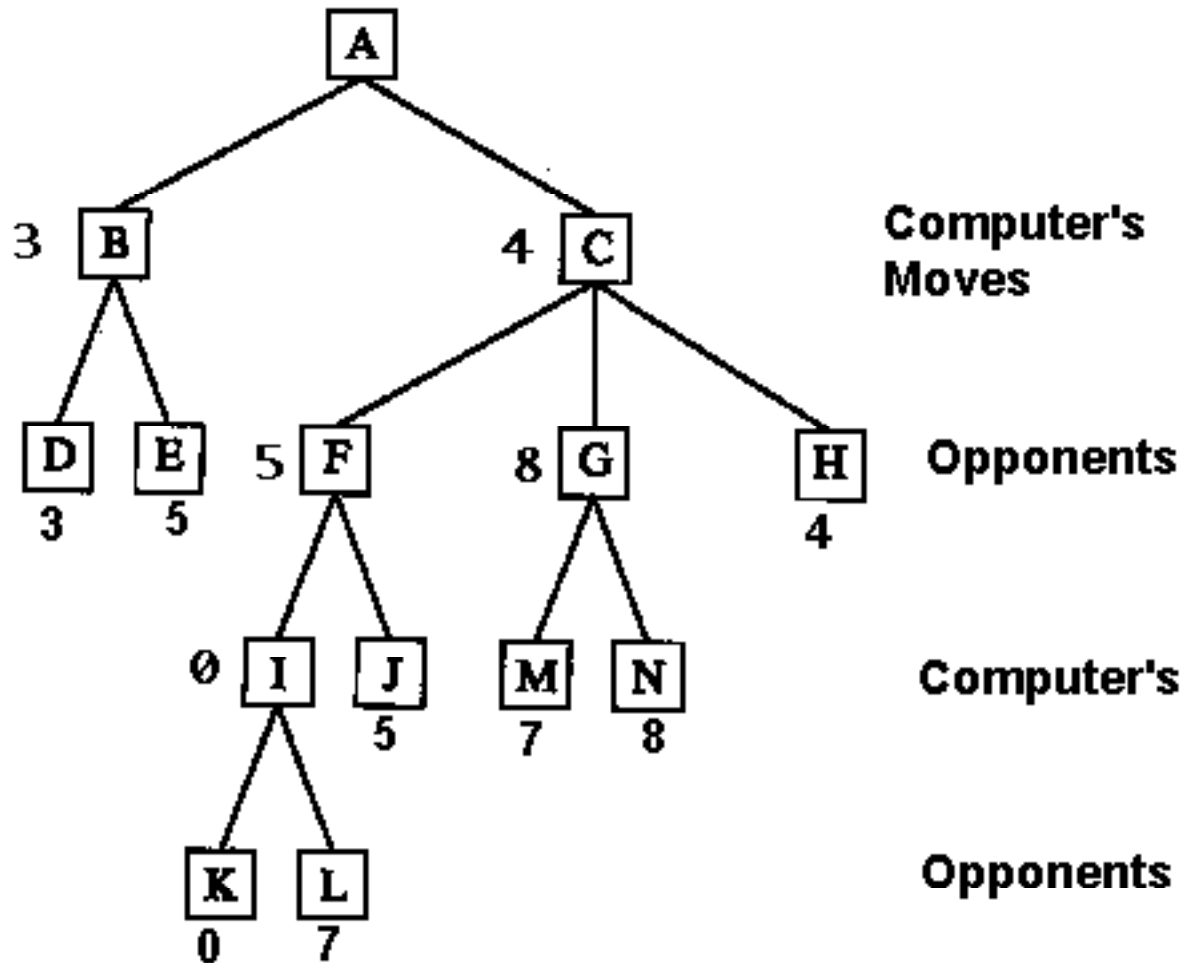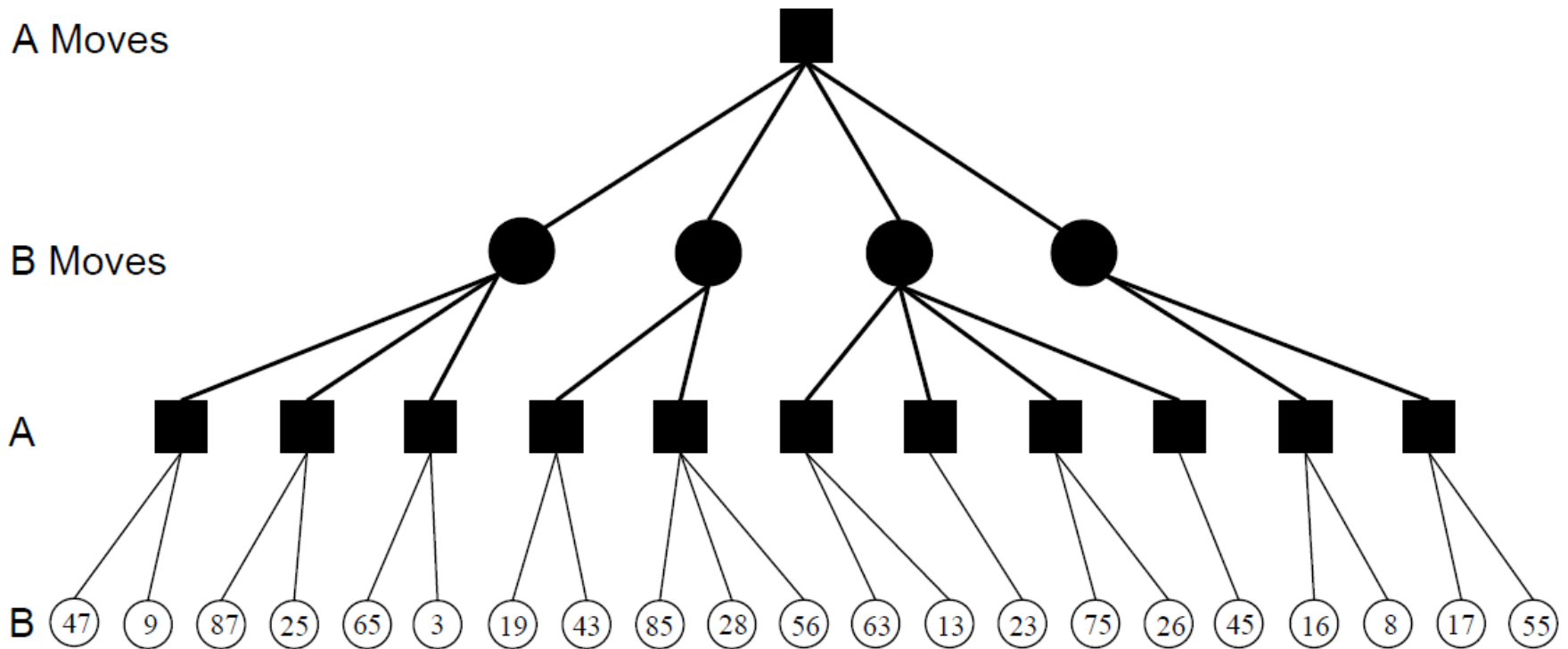
Admissible but not consistent

Chapter 5 (Games) Concepts

- Game tree
  - Players
  - Actions/moves
  - Terminal utility
  - MIN/MAX nodes
- MINIMAX algorithm
- Alpha/Beta pruning
  - Effect of node/move ordering on pruning
- Evaluation functions
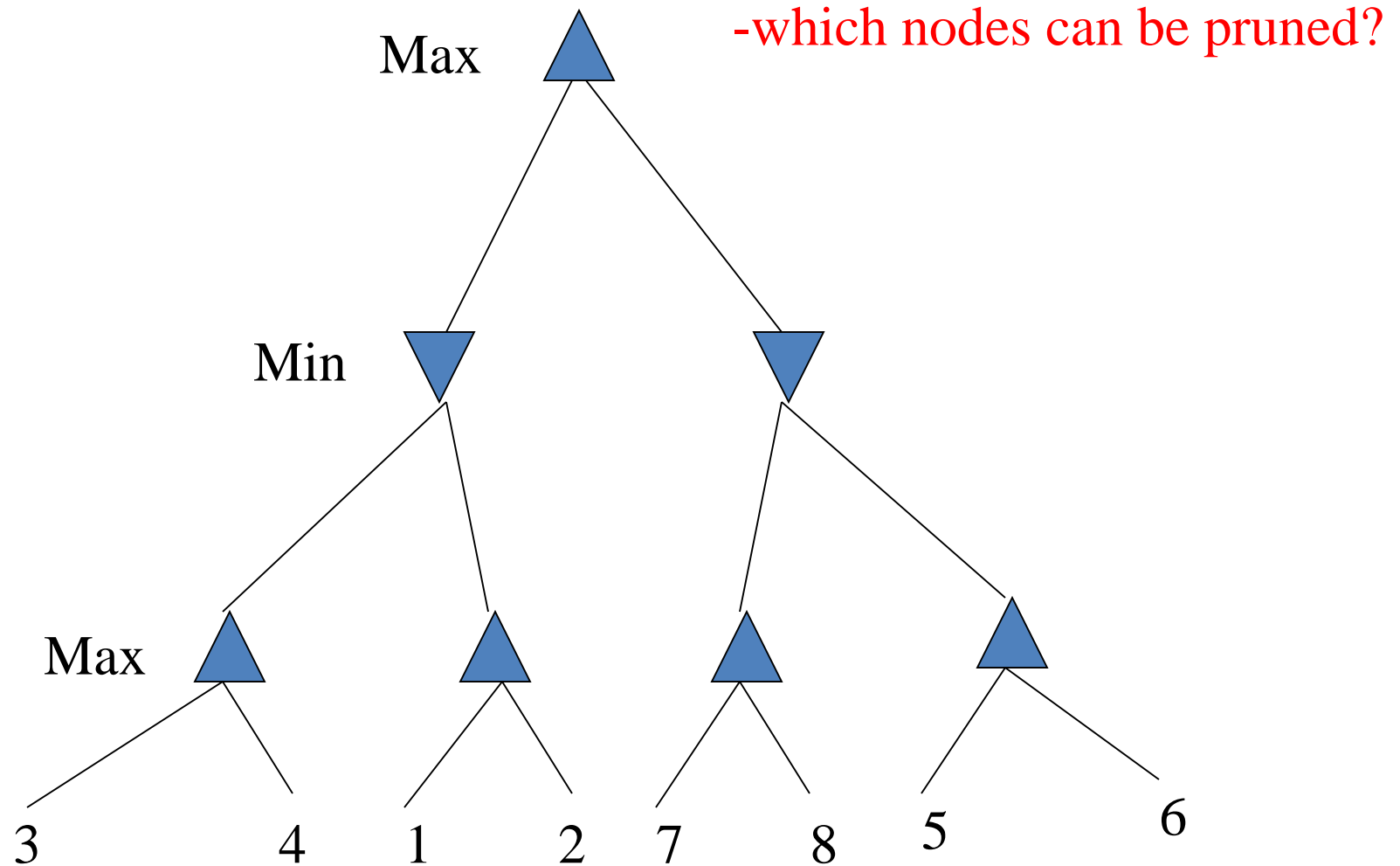 - Why do we need them?
- Stochastic games

A Game tree

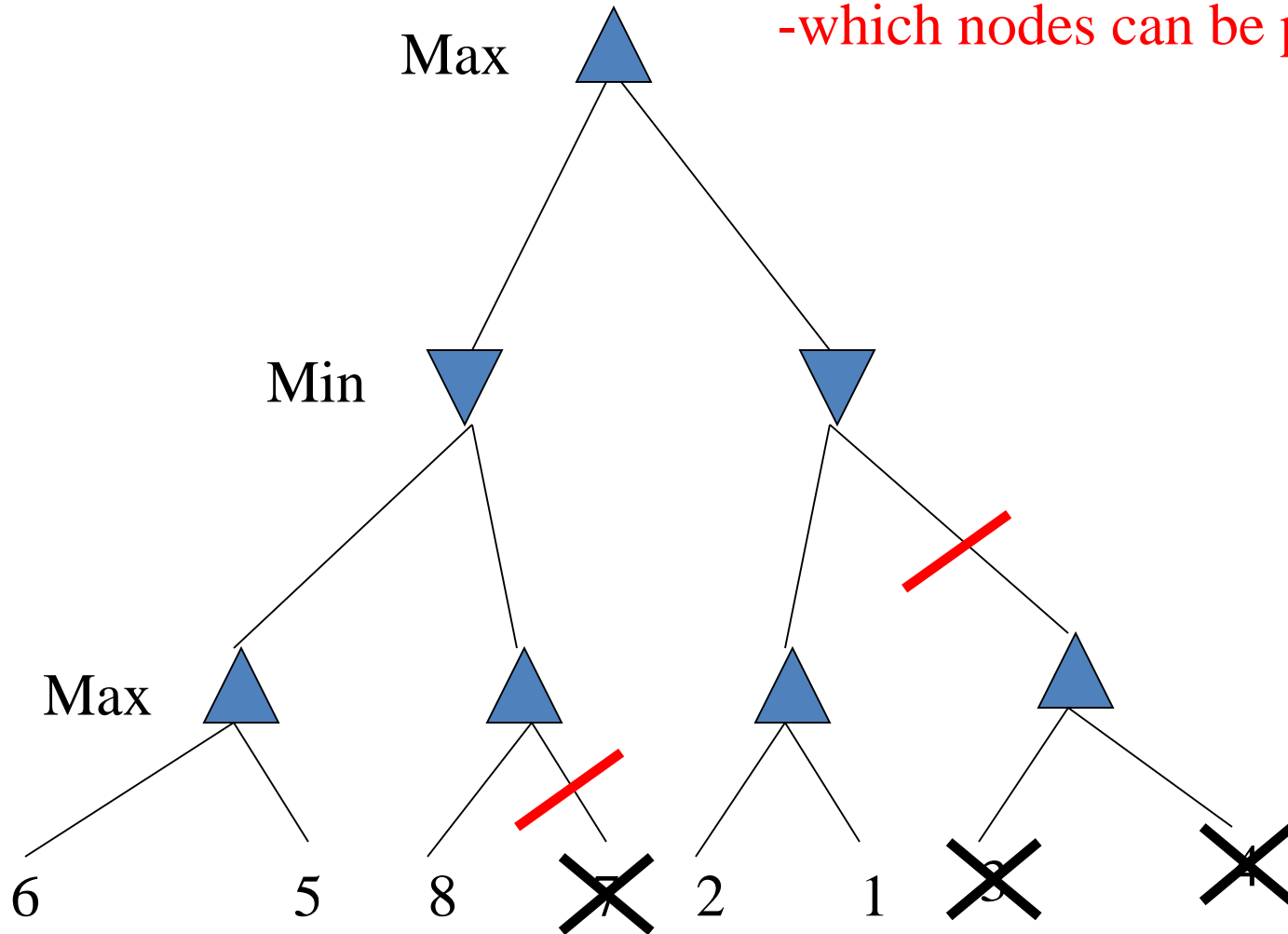# Another game tree

Answer to Example

Max

Min

Max

3   4   1   2   7   8   5   6

Answer: NONE! Because the most favorable nodes for both are explored last (i.e., in the diagram, are on the right-hand side).

Answer to Second Example
(the exact mirror image of the first example)
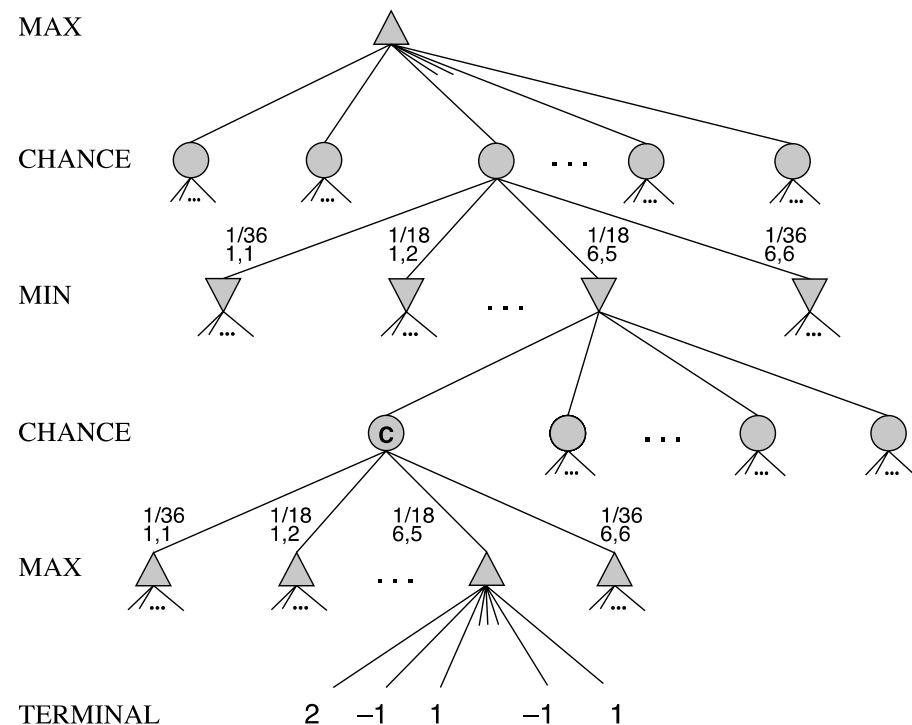
-which nodes can be pruned?

Max

Min

Max

6   5   8   ✗   2   1   ✗   ✗

Answer: LOTS! Because the most favorable nodes for both are explored first (i.e., in the diagram, are on the left-hand side).

Schematic Game Tree for Backgammon Position

MAX

CHANCE

MIN

CHANCE

MAX

TERMINAL

1/36 1,1   1/18 1,2   1/18 6,5   1/36 6,6

1/36 1,1   1/18 1,2   1/18 6,5   1/36 6,6

2   −1   1   −1   1

- How do we evaluate good move?
- By expected utility leading to expected minimax
- Utility for max is highest expected value of child nodes
- Utility of min-nodes is the lowest expected value of child nodes
- Chance node take the expected value of their child nodes.

- Try Monte-Carlo here!!!

Chapter 6 (CSP) Concepts

- Language : variables, domains, constraints
  - a solution : assignment of values to variables so that all constraints are satisfied
- Constraint graph
- Local consistency
  - Arc-consistency, path-consistency, k-consistency
- Backtracking search
  - (Q : how is BT search different from DFS?)
  - Variable, value ordering heuristics
- Interleaving search and inference
  - E.g. BT with arc-consistency
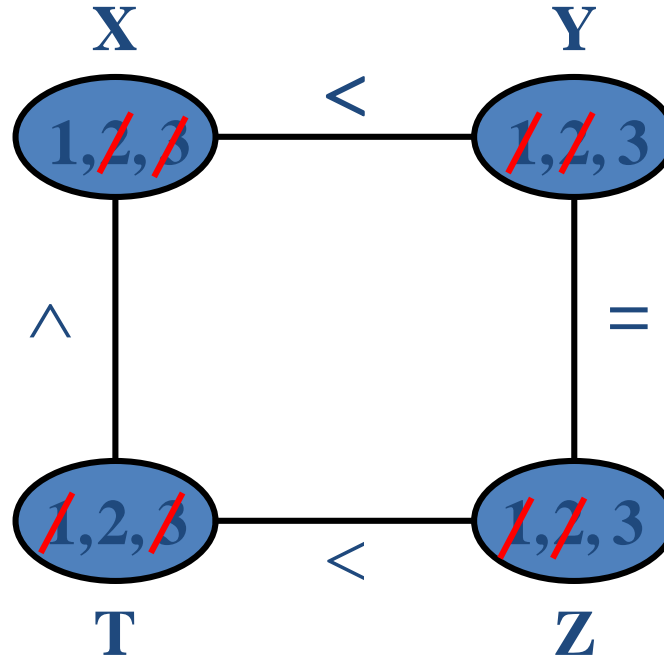- Greedy local search
  - Min-conflicts

Arc-consistency

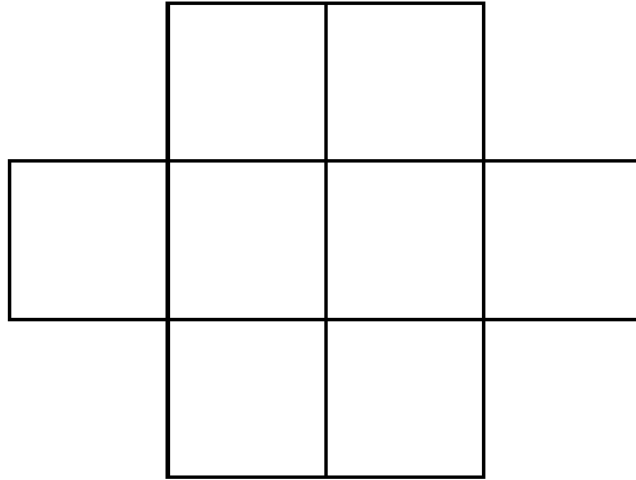$1 \leq X, Y, Z, T \leq 3$
$X < Y$
$Y = Z$
$T < Z$
$X < T$

A Constraint problem

The task is to label the boxes above with the numbers 1-8 such that the labels of any pair of adjacent squares (i.e. horizontal vertical or diagonal) differ by at least 2 (i.e. 2 or more).

(a) Write the constraints in a relational form and draw the constraint graph.

(b) Is the network arc-consistent ? if not, compute the arc-consistent network.
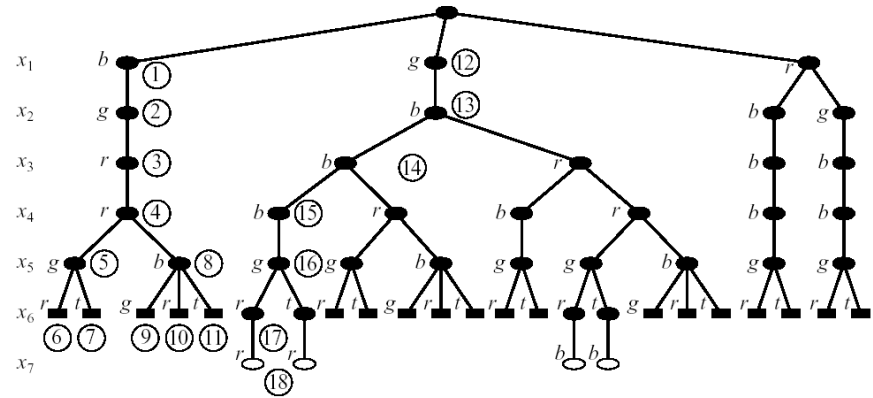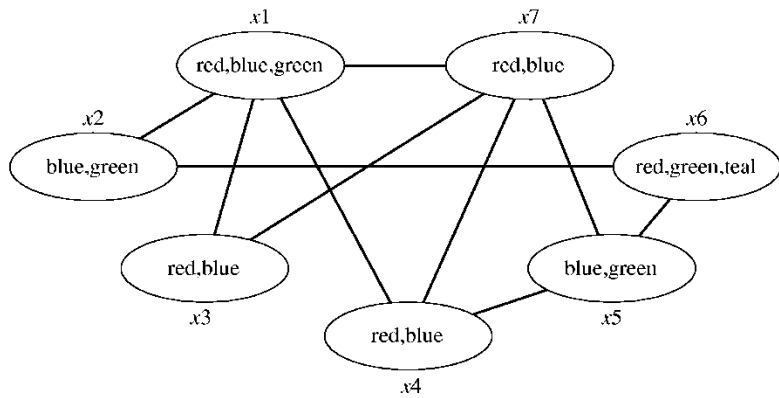
(c) Is the network consistent ? If yes, give a solution.

The effect of variable ordering

z divides x, y and t

(a)

(b)

(c)
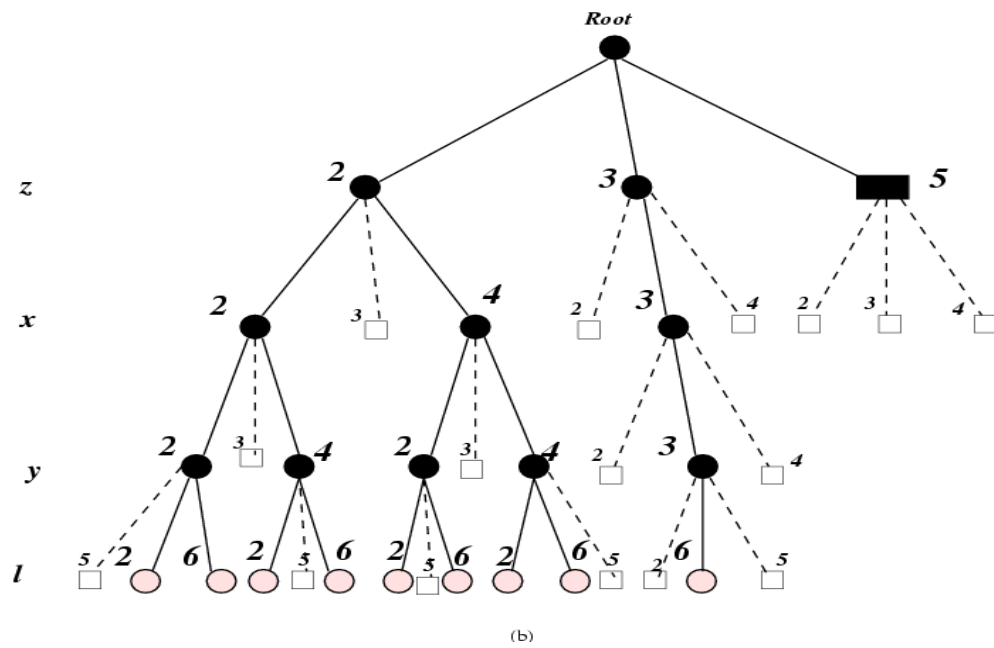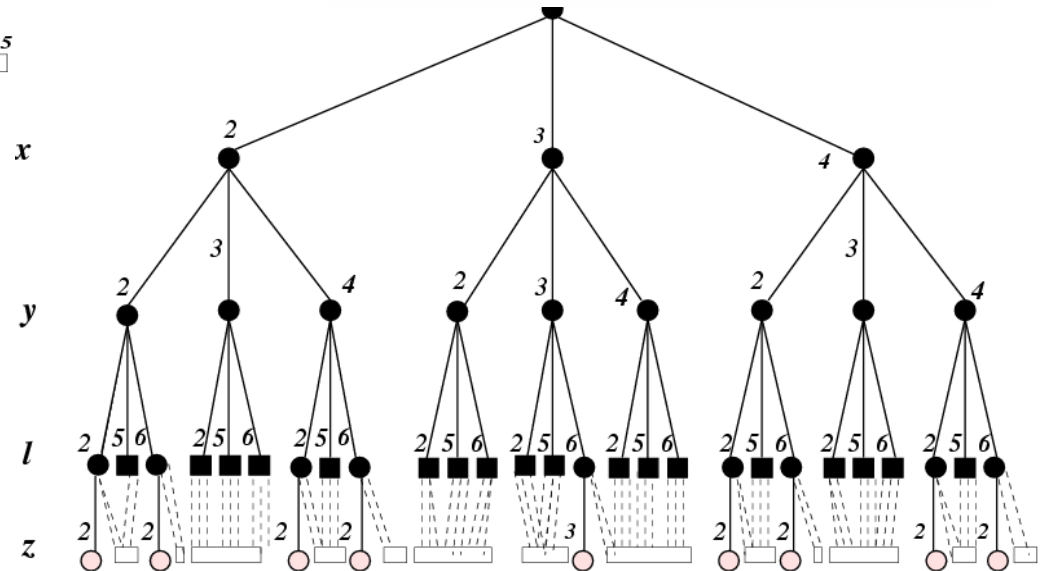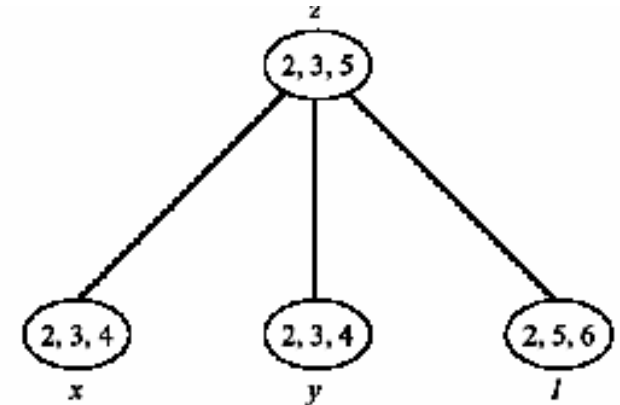
Backtracking Search for a Solution

(a)

(b)
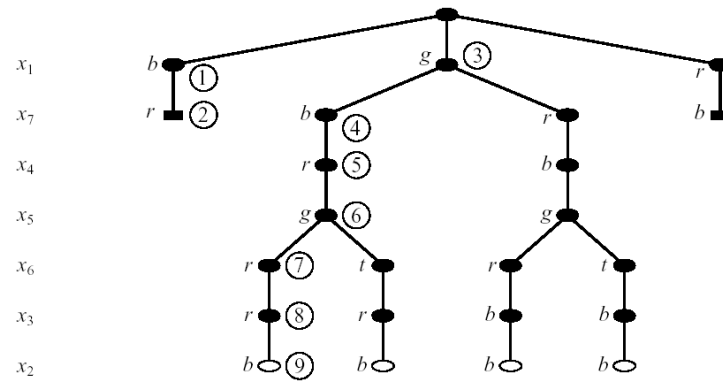
Min-Conflicts

At each step, find globally minimizing move!

Chapter 7 (Prop Logic) Concepts

- Syntax : propositional symbols; logical connectives
- Semantics
  - Worlds, models
  - Entailment
  - Inference
  - Soundness/Completeness
  - Validity/Satisfiability
- Model checking
- Modus Ponens
- CNF
- Horn clauses, Forward/Backward chaining
- Resolution
- DPLL backtracking search

Forward chaining

- Idea: fire any rule whose premises are satisfied in the *KB*,
    - add its conclusion to the *KB*, until query is found

$$P \Rightarrow Q$$
$$L \wedge M \Rightarrow P$$
$$B \wedge L \Rightarrow M$$
$$A \wedge P \Rightarrow L$$
$$A \wedge B \Rightarrow L$$
$$A$$
$$B$$
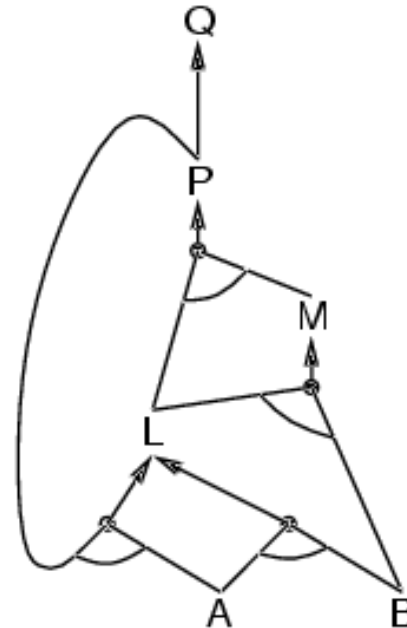
Backward chaining example
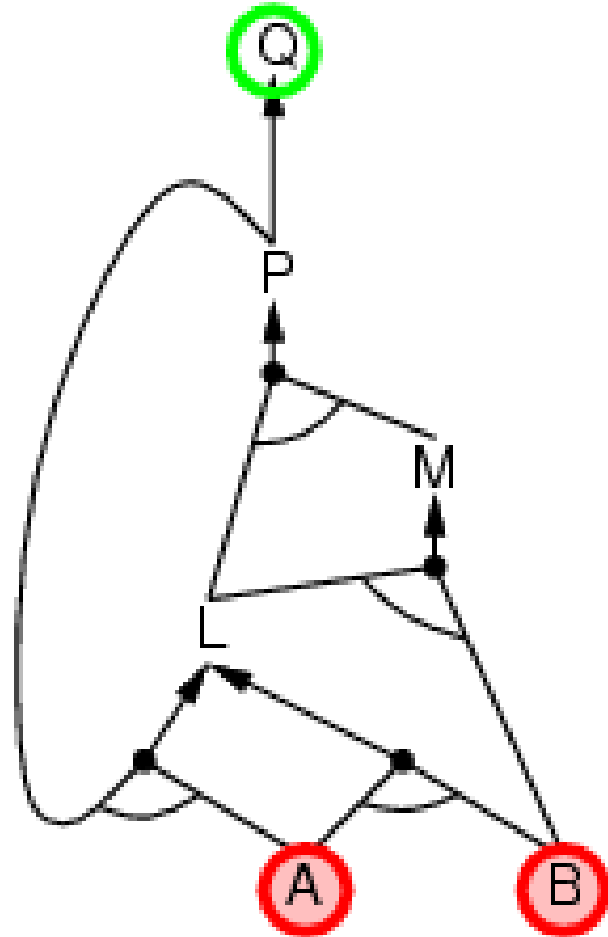
$$P \Rightarrow Q$$
$$L \wedge M \Rightarrow P$$
$$B \wedge L \Rightarrow M$$
$$A \wedge P \Rightarrow L$$
$$A \wedge B \Rightarrow L$$
$$A$$
$$B$$
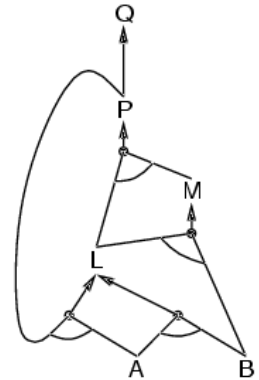
Resolution example

- $KB = (B_{1,1} \Leftrightarrow (P_{1,2} \vee P_{2,1})) \wedge \neg B_{1,1}, \quad \alpha = \neg P_{1,2}$
- Convert KB/neg-query to CNF
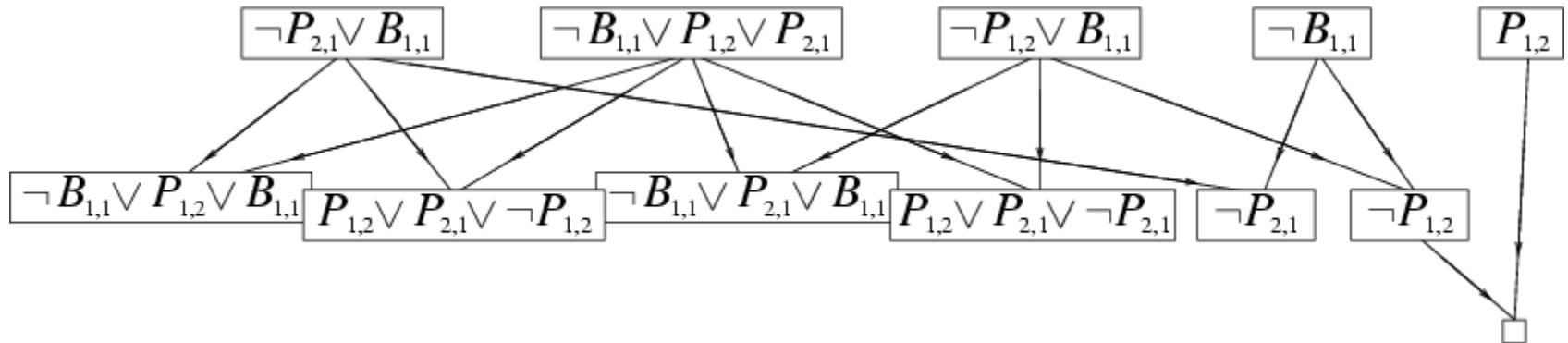
Chapters 8,9 (FOL) Language

- Syntax
  - Variables, const symbols, fn symbols, predicate symbols
  - Terms, atomic sentences
  - Quantifiers
- Semantics
  - Model, interpretation
  - Entailment

Chapters 8,9 (FOL) Inference

- Universal, existential instantiation
- Unification
- Generalized Modus Ponens
  - Definite clauses
- Converting a FOL sentence to CNF
- Inference algorithms
  - Forward Chaining
  - Backward Chaining
  - Resolution (answer extraction)

FOL Resolution Problem

(Problem 16.10 from Nillson) Use resolution refutation on a set of clauses to prove that there is a green object if we are given:

- If pushable objects are blue, then nonpushable ones are green.
- All objects are either blue or green but not both.
- If there is a nonpushable object, then all pushable ones are blue.
- Object 01 is pushable.
- Object 02 is not pushable.

(a) Convert these statements to expressions in first-order predicate calculus.

(b) Convert the preceding predicate-calculus expressions to clause form.

(c) Combine the preceding clause form expressions with the clause form of the negation of the statement to be proved, and then show the steps used in obtaining a resolution refutation

(d) Use resolution-answer-extraction to find a particular object that is green

Chapter 10 (Planning) Concepts

- STRIPS (PDDL) language
  - Factored representation of states
  - Actions (schema) : PreCondition, Effects lists
- Planning as Forward/Backward search
- Heuristics for planning, relaxed problem idea
  - Ignore PC, neg effects, etc.
  - Abstraction
- Planning graphs : construction, properties
  - Using planning graphs for heuristic computation
- Planning as satisfiability

STRIPS/PDDL

$Init(On(A, Table) \land On(B, Table) \land On(C, Table)$
$\quad \land Block(A) \land Block(B) \land Block(C)$
$\quad \land Clear(A) \land Clear(B) \land Clear(C))$
$Goal(On(A, B) \land On(B, C))$
$Action(Move(b, x, y),$
$\quad$ PRECOND: $On(b, x) \land Clear(b) \land Clear(y) \land Block(b) \land$
$\quad\quad\quad (b \neq x) \land (b \neq y) \land (x \neq y),$
$\quad$ EFFECT: $On(b, y) \land Clear(x) \land \neg On(b, x) \land \neg Clear(y))$
$Action(MoveToTable(b, x),$
$\quad$ PRECOND: $On(b, x) \land Clear(b) \land Block(b) \land (b \neq x),$
$\quad$ EFFECT: $On(b, Table) \land Clear(x) \land \neg On(b, x))$

Figure 11.4   A planning problem in the blocks world: building a three-block tower. One solution is the sequence $[Move(B, Table, C), Move(A, Table, B)]$.

Planning as Satisfiability

- Propositionalize actions
- Define initial state (F/$\neg$F for everything given/unknown)
- Pick plan length K
- Propositionalize the goal; assert goal at time k+1
- Add precondition/effect axioms
  - $A^k \rightarrow$ Preconditions(A^k) $\wedge$ Effects(A^{k+1})
- Add successor-state axioms; for each fluent F
  - $\neg F^k \wedge F^{k+1} \rightarrow$ ActionCausesF^{k+1}
- Add action exclusion axioms
  - Exactly one action at a time (can have NoOP)